

Constraints on Axion-like Particles from a Hard X -ray Observation of Betelgeuse

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We use the first observation of Betelgeuse in hard X -rays to perform a novel search for axion-like particles (ALPs). Betelgeuse is not expected to be a standard source of X -rays, but light ALPs produced in the stellar core could be converted back into photons in the Galactic magnetic field, producing a detectable flux that peaks in the hard X -ray band ($E_\gamma > 10$ keV). Using a 50 ks observation of Betelgeuse by the *NuSTAR* satellite telescope, we find no significant excess of events above the expected background. Using models of the regular Galactic magnetic field in the direction of Betelgeuse, we set a 95% C.L. upper limit on the ALP-photon coupling of $g_{a\gamma} < (0.5 - 1.8) \times 10^{-11}$ GeV⁻¹ (depending on magnetic field model) for ALP masses $m_a < (5.5 - 3.5) \times 10^{-11}$ eV.

Introduction.—Axion-like particles (ALPs) are ultralight pseudoscalar bosons with a two-photon vertex $g_{a\gamma}$, predicted by several extensions of the Standard Model (see [1, 2] for a recent review). In the presence of an external magnetic field, the $g_{a\gamma}$ coupling leads to the phenomenon of photon-ALP mixing [3]. This effect is exploited by several ongoing and upcoming ALP search experiments (see [1, 4, 5] for recent reviews).

The photon-ALP coupling would also cause ALPs to be produced in stellar plasmas via the Primakoff process [6]. Therefore astrophysical observations offer unique sensitivity to ALPs. Analyses of the lifetime of helium-burning stars in globular clusters have excluded the couplings $g_{a\gamma} > 6 \times 10^{-11}$ GeV⁻¹ (95% confidence level, C.L.) for $m_a \lesssim 30$ keV [7–9]. This is the strongest bound on the ALP-photon coupling in a wide mass range. A comparable bound, $g_{a\gamma} > 6.6 \times 10^{-11}$ GeV⁻¹ (95% C.L.) for $m_a \lesssim 0.02$ eV, was derived by the CAST experiment, which searches for ALPs produced in the Solar core that are re-converted into X -rays in a large laboratory magnetic field [10].

At lower ALP masses, as shown in Fig. 1, more stringent bounds are derived from supernovae and galaxy cluster observations. A recent reanalysis of the SN 1987A limit, derived from the non-observation of gamma-rays induced by conversion in the Galactic magnetic field of ALPs produced in the supernova core, excludes $g_{a\gamma} > 5.3 \times 10^{-12}$ GeV⁻¹ for $m_a < 4.4 \times 10^{-10}$ eV (95% C.L.) [11]. A search for gamma-ray bursts from extra-galactic supernovae with the Fermi Large Area Telescope (LAT) has yielded a weaker limit, $g_{a\gamma} \lesssim 2.6 \times 10^{-11}$ GeV⁻¹ for ALP masses $m_a \lesssim 3 \times 10^{-10}$ eV [12], under the assumption of at least one supernova occur-

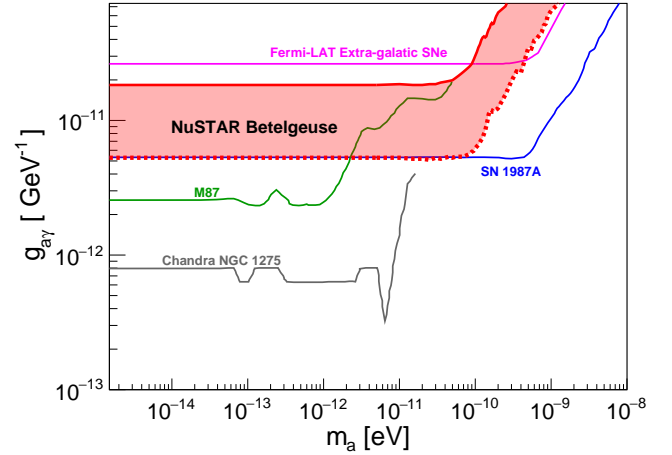


FIG. 1. Astrophysical constraints on the ALP-photon coupling in relation to the Betelgeuse bound from the present work: SN 1987A [11], Fermi-LAT extra-galactic SNe [12], M87 [14], and Chandra NGC 1275 [15].

ring in the LAT field of view. However, the SN 1987A bound has been questioned due to uncertainties on the response of the GRS instrument on the SMM satellite [13], and both of these bounds are subject to uncertainties due to the modeling of core-collapse supernovae and Galactic magnetic fields. The most stringent limits to date on low-mass ALPs come from the search for X -ray spectral distortions in the active galactic nucleus NGC 1275 at the center of the Perseus cluster, induced by conversion in the intra-cluster medium. These exclude $g_{a\gamma} > (6 - 8) \times 10^{-13}$ GeV⁻¹ (99.7% C.L.) for $m_a < 10^{-12}$ eV [15]. However, these results could be

weakened by several orders of magnitude if the intra-cluster magnetic field has been mis-modeled [16].

Here, we exploit the fact that Betelgeuse, a nearby red supergiant star, provides an excellent laboratory for ALPs, as proposed in a seminal paper by E. Carlson [17]. Betelgeuse (α Orionis, spectral type M2Iab) is an ideal candidate for ALP searches, as it (i) has a hot core, and thus is potentially a copious producer of ALPs that, after re-conversion in the Galactic magnetic field, produces a photon signal peaked in the hard X -ray range, and (ii) is in region of Hertzsprung-Russel diagram where no stable corona is expected, and thus has essentially zero standard astrophysical X -ray background [18]. This basic idea can be extended to other stellar objects, such as clusters of hot, young stars [19]. Betelgeuse has the additional advantage that it is nearby, at a distance $d \sim 200$ pc [20, 21], and thus in a region of the local magnetic field that is relatively easier to constrain with future observations.

In this work, we use a dedicated observation of Betelgeuse by the *NuSTAR* satellite telescope to derive limits on the ALP-photon coupling $g_{a\gamma} < (0.5 - 1.8) \times 10^{-11} \text{ GeV}^{-1}$ (95% C.L.) for masses $m_a < (5.5 - 3.5) \times 10^{-11} \text{ eV}$ (depending on the assumed value of the regular Galactic magnetic field). We derive a range of ALP spectra expected from Betelgeuse, depending on its precise evolutionary stage. We then derive the expected X -ray spectra after conversion in the regular Galactic magnetic field, and compare to our spectral measurement in the energy range 3–79 keV. For low-mass ALPs, these limits are a factor of ~ 3 deeper than the limits from CAST, and are comparable to the limits expected from next-generation ALP experiments such as ALPS-II [22] and BabyIAXO [23, 24]. They are competitive with the constraints from SN 1987A, though with independent sources of systematic uncertainty. We emphasize that the preponderance of astrophysical exclusions that overlap in this region of $g_{a\gamma} - m_a$ parameter space, each with a separate modeling assumptions and sources of uncertainty, builds confidence in the robustness of these constraints. *ALP and photon fluxes from Betelgeuse.*—In the minimal scenarios, ALPs have only a two-photon coupling, described by the Lagrangian [3]:

$$\mathcal{L}_{a\gamma} = -\frac{1}{4} F_{\mu\nu} \tilde{F}^{\mu\nu} a = \mathbf{E} \cdot \mathbf{B} a . \quad (1)$$

This interaction allows for ALP production in a stellar medium primarily through the Primakoff process, in which thermal photons are converted into ALPs in the electrostatic field of ions, electrons and protons. The ALP production rate via the Primakoff process in a stellar core can be calculated as (see, e.g., [17]),

$$\frac{d\dot{n}_a}{dE} = \frac{g_{a\gamma}^2 \xi^2 T^3 E^2}{8\pi^3 (e^{E/T} - 1)} \left[\left(1 + \frac{\xi^2 T^2}{E^2} \right) \ln \left(1 + \frac{E^2}{\xi^2 T^2} \right) - 1 \right] , \quad (2)$$

where E is the photon energy, T the temperature, and $\xi^2 = \kappa^2/4T^2$ with κ the inverse of the screening length, introduced by the finite range of electric field surrounding charged particles in the plasma. Once produced, ALPs can easily escape the star since their mean free path in stellar matter is sufficiently large for the values of mass and coupling we are interested in. The total ALP spectrum can then be obtained by integrating Eq. (2) over the volume of the star, $d\dot{N}_a/dE = \int (d\dot{n}_a/dE) dV$, which can be well parametrized by fitting the stellar model (see Supplementary Material for details).

The ALP spectrum thus depends on the physical structure and chemical evolution of the star. Betelgeuse, due to its relative proximity, has fairly well-constrained observed values of luminosity, effective temperature, and metallicity (see Supplementary Material). However, the time until core-collapse is not well known, and as the temperature and density of the core increase as the star approaches supernova, this introduces significant uncertainty on the predicted ALP spectra. We use the Full Network Stellar evolution code (FuNS [25]) to derive 13 models of the Betelgeuse ALP source spectrum, parametrized by the time until core-collapse, t_{cc} . These range from an optimistic ALP production scenario ($t_{cc} = 1.4$ yr) to a conservative ALP flux scenario ($t_{cc} = 1.55 \times 10^5$ yr), as shown in Tab. S1.

The interaction in Eq. (1) may also trigger ALP-photon oscillations in external magnetic fields, such as those found in our galaxy, thus producing a detectable X -ray flux. The calculation of the ALP-photon re-conversion probability simplifies if we restrict ourselves to the case in which \mathbf{B} is homogeneous. The magnetic field of the Galaxy is known to change on scales of ~ 1 kpc, corresponding to the arm and inter-arm regions, and between the Galactic disk and halo [26–28]. Motivated by the relative proximity of Betelgeuse in the Galactic disk, we assume conversion in a homogenous regular magnetic field. Although the magnetic structure of the Galaxy is certainly more complex – including turbulent fields with coherent lengths $\mathcal{O}(200 \text{ pc})$ or smaller [28–30], such as due to supernovae, molecular clouds, and our own Local Bubble – this assumption follows the convention of previous astrophysical bounds, e.g. SN 1987A [11]. This allows for consistent comparison between constraints. A detailed treatment of the effect of magnetic field correlations lengths and amplitudes on the conversion probability is deferred to a later dedicated theoretical study.

In this framework, the differential photon flux per unit energy arriving at Earth is

$$\frac{dN_\gamma}{dEdSdt} = \frac{1}{4\pi d^2} \frac{d\dot{N}_a}{dE} P_{a\gamma} . \quad (3)$$

The ALP-photon conversion probability is [31]:

$$P_{a\gamma} = 8.7 \times 10^{-6} g_{11}^2 \left(\frac{B_\Gamma}{1 \mu\text{G}} \right)^2 \left(\frac{d}{197 \text{ pc}} \right)^2 \frac{\sin^2 q}{q^2} , \quad (4)$$

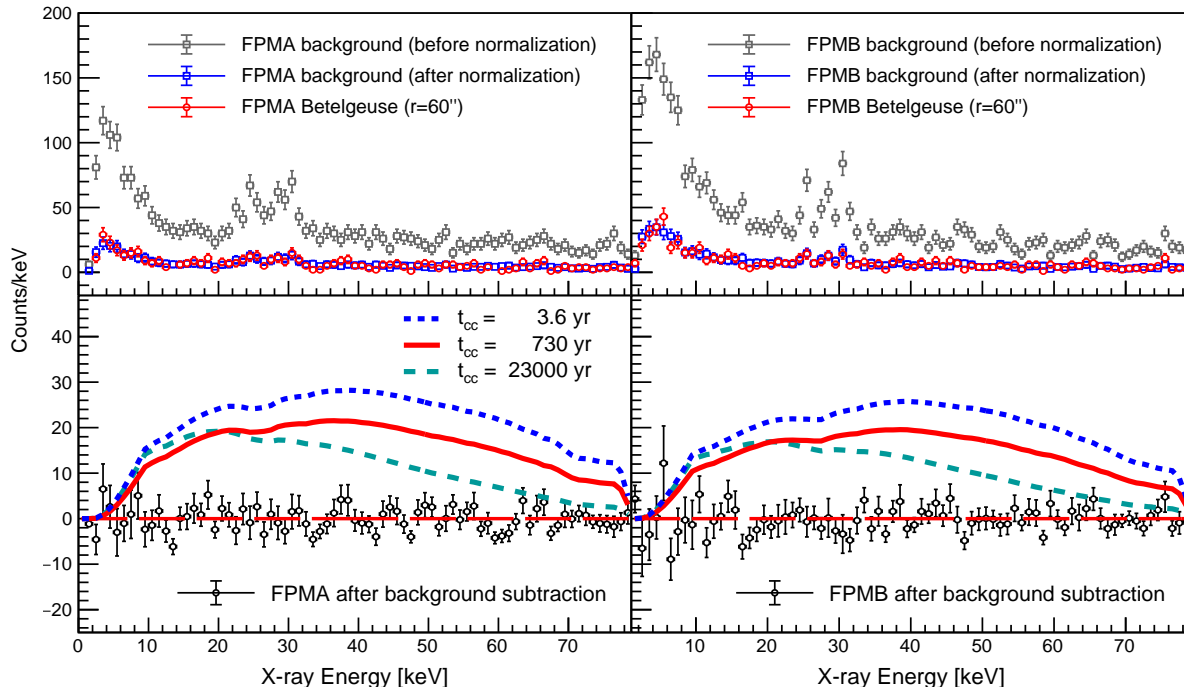


FIG. 2. *Top*: X-ray spectra from FPMA (*left*) and FPMB (*right*) for the Betelgeuse source (red) and background (gray and blue for before and after normalization) regions. The error bars overlaid are the statistic uncertainties (\sqrt{N}). *Bottom*: Source spectra after subtracting the normalized background. The error bars are calculated by Sumw2 with ROOT software [41]. The predicted ALP-produced X-ray spectra assuming transverse magnetic field $B_T = 1.4 \mu\text{G}$, mass $m_a = 10^{-11} \text{eV}$ and coupling $g_{a\gamma} = 1.5 \times 10^{-11} \text{GeV}^{-1}$, that would be detected by the *NuSTAR* instrument are overlaid. The stellar model parameters are described in Tab. S1. The spectra are binned to a width of 1 keV, though analysis is performed on unbinned data.

where B_T is the transverse magnetic field, namely its component in the plane normal to the path between Earth and Betelgeuse, q is the momentum transfer, and d is the magnetic field length.

$$q \simeq \left[77 \left(\frac{m_a}{10^{-10} \text{eV}} \right)^2 - 0.14 \left(\frac{n_e}{0.013 \text{cm}^{-3}} \right) \right] \times \left(\frac{d}{197 \text{pc}} \right) \left(\frac{E}{1 \text{keV}} \right)^{-1}, \quad (5)$$

n_e is the electron density [32]. Practically, the differential photon flux per unit energy arriving at Earth can be numerically calculated by Eq. (S2) where the parameters are fitted with stellar evolution model and listed in Tab. S1. The predicted ALP-photon spectra are illustrated in Fig. S2.

For small values of q (small ALP mass) and our assumed homogenous \mathbf{B} field, the expected ALP flux does not depend strongly on the distance to the source, as the drop in flux with distance is compensated by an increase in the conversion probability (Eq. (4–5)). Thus we ignore any uncertainty due to the distance to Betelgeuse for the small ALP masses considered here. For large q (for large ALP mass), the increase in the conversion probability with the distance is lost because of incoherence effects.

Even within the simplifying assumption of a uniform regular magnetic field, the exact value of the magnetic field in the direction of Betelgeuse introduces a considerable source of uncertainty in our estimate of the X-ray flux. The reported values of the local regular magnetic field, translated to B_T in the direction of Betelgeuse, vary between $0.4 \mu\text{G}$ [27] and $3.0 \mu\text{G}$ [33]. Here we are using $1.4 \mu\text{G}$ [28] as a representative value and $0.4 \mu\text{G}$ and $3.0 \mu\text{G}$ as the lower and upper bound.

Spectral analysis.—The *NuSTAR* observatory [34–37] is the first focusing high-energy X-ray telescope in orbit. Its 3–79 keV energy range is ideal for probing ALP signals from Betelgeuse. *NuSTAR* has two identical co-aligned telescopes, each consisting of an independent optic and focal-plane detector, referred to as FPMA and FPMB. Each telescope subtends a field-of-view of approximately $13' \times 13'$, with a half-power diameter of $\sim 60''$ for a point source near the optical axis.

We use a dedicated *NuSTAR* observation of Betelgeuse taken on 23 August 2019 (ObsID 30501012002). We processed the data using the standard *NuSTAR* data reduction pipeline, NUSTARDAS v1.8.1 distributed in HEASOFT v6.24, and the latest calibration package (CALDB.indx20191219). We used the flags

SAAMODE=OPTIMIZED and TENTACLE=YES to exclude time intervals with elevated instrument backgrounds, coinciding with the telescope passing through the South Atlantic Anomaly (SAA). After this filtering, the total cleaned exposure was 49.2 ks for FPMA, and 48.4 ks for FPMB.

We extract spectra with NUPRODUCTS, using a circular source region of radius $60''$ around the star's equatorial coordinates (RA 88.79293° , Dec. 7.40706°) [38]. We simultaneously extract the instrument response files used to generate the ALP signal spectra that would be observed in this same region, in particular the Auxiliary Response File (ARF) which defines the energy-dependent effective area for this source region, and the Redistribution Matrix File (RMF) which contains the detector quantum efficiency and energy resolution [34].

We extract background spectra from nearby regions, as shown in Fig. S3. These regions are separated from the center of the source region by at least $120''$ in order to ensure that contamination from the source region is below the level of $\mathcal{O}(1\%)$. In addition, we observe a point source near the edge of both FPMs, whose position is consistent with Chandra source CXO J055520.2+072002 [39]. This source is not detected above 10 keV, but to be conservative we choose the background region to be at least $60''$ from this object. The background region is chosen to be on the same detector chip as the source region, in order to properly describe any spatially-varying backgrounds. In particular, the *NuSTAR* instrumental background, including X-ray lines resulting from fluorescence/activation of the instrument materials, is known to vary between detector chips, and the stray light from the cosmic X-ray background varies radially along the detector plane [40]. Our results are robust to alternate choices of background region, as shown in the Supplementary Material.

The observed X-ray spectra for FPMA and FPMB in the source region and background region are shown in top panel of Fig. 2. Both source and background rates are higher for FPMB than for FPMA, due to the higher instrumental background in this detector. The background-subtracted source spectra are shown in the lower panel of Fig. 2. These were prepared by normalizing the background spectra by the area of the source extraction region, following the procedure in NUPRODUCTS. After background subtraction, the source spectrum fluctuates around zero counts. We confirm that our upper limit on the background-subtracted count rate from Betelgeuse is consistent with that measured in soft X-rays (0.3–8 keV) using data from *Chandra* (see the Supplementary Material).

The source spectra after the background subtraction is compared to examples of the predicted X-ray spectra from ALP production, for the case of $B_T = 1.4 \mu\text{G}$, $m_a = 10^{-11} \text{ eV}$ and $g_{a\gamma} = 1.5 \times 10^{-11} \text{ GeV}^{-1}$, also shown in the lower panel of Fig. 2. We numerically calculate the ALP-produced photon spectrum dN_γ/dE_γ that would be

Photon Energy	FPMA		FPMB	
	N_{obs}	N_{bkg}	N_{obs}	N_{bkg}
10–60 keV	313	315.8	352	362.7
10–70 keV	354	359.8	397	406.4
10–79 keV	384	392.7	433	441.2

TABLE I. Observed events in the source region and expected background events, after normalization to the source region area, for FPMA and FPMB.

detected by *NuSTAR* by folding the predicted spectrum from Eq. (S2) through the instrument response files extracted by NUPRODUCTS for this source region.

Data analysis and results.—Based on the predicted number of photons from ALPs (N_{ax}) and the expected number of background events (N_{bkg}) in our source region, we first optimized the energy range used for our analysis by maximizing the figure-of-merit $N_{\text{ax}}/\sqrt{N_{\text{bkg}}}$. This was done before inspecting our source data. Because of the difference in shape for the predicted ALP spectra, we use three different energy ranges: 10–60 keV for the model with $t_{\text{cc}} = 1.55 \times 10^5 \text{ yr}$, 10–70 keV for $t_{\text{cc}} = 6900\text{--}23000 \text{ yr}$, and 10–79 keV for $t_{\text{cc}} = 1.4\text{--}3700 \text{ yr}$. The number of source events (N_{obs}) and expected background events (N_{bkg}) in the optimized energy ranges for FPMA and FPMB are listed in Tab. I. The observed events in Betelgeuse source region are consistent with the expected background events within the statistic uncertainties for both FPMA and FPMB.

To fit the data, an unbinned likelihood function is constructed as [42]

$$\mathcal{L} = \prod_{i=1}^n \mathcal{L}_i \times \prod_{i=1}^n \text{Gauss}(\delta_{\text{bkg}}^i, \sigma_{\text{bkg}}^i), \quad (6)$$

where

$$\begin{aligned} \mathcal{L}_i = & \text{Poisson}(N_{\text{obs}}|N_{\text{exp}}) \\ & \times \prod_{j=1}^{N_{\text{obs}}} \left[\frac{N_{\text{ax}} P_{\text{ax}}(E_\gamma^j)}{N_{\text{exp}}} + \frac{N_{\text{bkg}}(1 + \delta_{\text{bkg}}) P_{\text{bkg}}(E_\gamma^j)}{N_{\text{exp}}} \right] \end{aligned} \quad (7)$$

Here, N_{obs} is the total number of events observed in our source region, and $N_{\text{exp}} = N_{\text{ax}} + N_{\text{bkg}} \cdot (1 + \delta_{\text{bkg}})$ is the total number of events expected in our source region for the case of an ALP signal. $P_{\text{ax}}(E_\gamma)$ is the energy-dependent ALP signal PDF, defined for given m_a , $g_{a\gamma}$, t_{cc} , and B_T (examples are shown in the lower panel of Fig. 2 and Fig. S2). $P_{\text{bkg}}(E_\gamma)$ is the background PDF, obtained by normalizing the background spectrum to the source region size using NUPRODUCTS, as described above. δ_{bkg}

and σ_{bkg} are the nuisance parameter and fractional systematic uncertainty of the background; $\text{Gauss}(\delta_{\text{bkg}}, \sigma_{\text{bkg}})$ is the Gaussian penalty term. Given the statistics of expected background events in the observation region, σ_{bkg} is set at 10% for both FPMA and FPMB, but allowed with independent Gaussian fluctuation.

The standard profile likelihood test statistic [43, 44] is used to derive constraints on the ALP-photon coupling $g_{a\gamma}$. The test statistic q is defined as

$$q(g_{\text{test}}) = \begin{cases} -2 \ln \frac{\mathcal{L}_{\text{max}}(g_{\text{test}}, \hat{\theta})}{\mathcal{L}_{\text{max}}(g_{\text{best}}, \hat{\theta})}, & g_{\text{test}} \geq g_{\text{best}} \\ 0, & g_{\text{test}} < g_{\text{best}} \end{cases} \quad (8)$$

For each choice of m_a , t_{cc} , and B_T , we scan through the ALP-photon coupling g_{test} , and perform two maximum likelihood fits, one with the $g_{a\gamma}$ as its best fit value g_{best} , and the other with $g_{a\gamma}$ fixed at g_{test} . The nuisance parameters are all allowed to vary in both to achieve the best fit. We derive the 95% C.L. upper limit on $g_{a\gamma}$ assuming $q(g_{\text{test}})$ follows a half- χ^2 distribution with a single degree of freedom [43].

The main sources of uncertainty on the ALP signal are the choice of stellar model (t_{cc}) and assumed value of the transverse local Galactic magnetic field strength (B_T). Rather than accounting for these as nuisance parameters in the likelihood function, we derive separate 95% C.L. limits on $g_{a\gamma}$ for each of the 13 stellar models for each of our three assumed values of B_T .

The final 95% C.L. upper limit on $g_{a\gamma}$ is shown in Fig. 3 and Fig. 1. The region labeled in red is excluded by this work while the width of the light red band reflects the uncertainty due to choice of stellar model and B_T . Using our most conservative assumptions ($t_{\text{cc}} = 1.55 \times 10^5$ yr and $B_T = 0.4 \mu\text{G}$), we set an upper limit of $g_{a\gamma} < 1.8 \times 10^{-11} \text{GeV}^{-1}$ for $m_a < 3.5 \times 10^{-11}$ eV. In the scenario that predicts the highest ALP flux ($t_{\text{cc}} = 3.6$ yr and $B_T = 3.0 \mu\text{G}$), we derive an upper limit of $g_{a\gamma} < 5.2 \times 10^{-12} \text{GeV}^{-1}$ for $m_a < 5.5 \times 10^{-11}$ eV.

The uncertainty in our derived limit is dominated by our choice of B_T , since the ALP-photon conversion probability of Eq. (4) scales as B_T^2 . The separate contributions to the uncertainty are illustrated in Fig. 4, which shows the evolution of our derived $g_{a\gamma}$ for different t_{cc} . The solid black line is a fit to the $g_{a\gamma}$ derived for $B_T = 1.4 \mu\text{G}$, shown by the black points. The width of the magenta band then indicates the uncertainty due to our lower and upper bounds on B_T . The dependence on our assumed B_T is further illustrated in Fig. S6, where we show our constraint in terms of $\text{GeV}^{-1} \sqrt{\mu\text{G}}$ for our range of t_{cc} .

Conclusions and Discussions.—Fig. 3 shows the current theoretical and experimental ALP landscape. This includes the current constraints from CAST [10], ABRACADABRA-10cm [45], and cavity experiments such as ADMX [46]. The yellow band indicates the

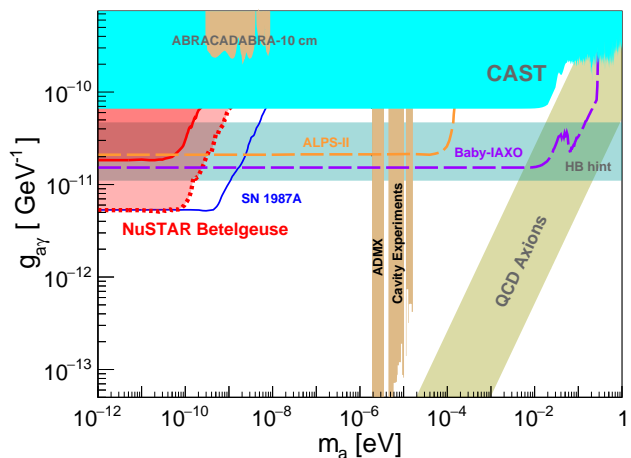


FIG. 3. Comparison of 95% upper limits of $g_{a\gamma}$ from *NuSTAR* Betelgeuse observation is shown in red band: upper solid line for the most conservative stellar model and B_T , lower dashed line for the most optimistic stellar model and B_T , and the interval for the other combinations. Overlaid are the region of interest for QCD axion [47], the current limits from CAST [10], ADMX [46], ABRACADABRA-10cm [45] and SN 1987A [11], the projected sensitivity of ALPS-II [22] and Baby-IAXO [23, 24]. Also labelled are the ALP regions suggested by hints of excess gamma-ray transparency or cooling of horizontal-branch stars [48, 49].

preferred region in which the axion couples to quantum chromodynamics (QCD) and could be a solution to the strong-CP problem [47], and the hatched band indicates the region where an ALP could explain the observed excess cooling of horizontal branch stars [48, 49]. The limits derived in this work exceed those set by CAST by a factor of ~ 3 for $m_a < 3.5 \times 10^{-11}$ eV, and are comparable in this low-mass space to the sensitivity of even next-generation experiments such as ALPS-II [22] and BabyIAXO [23, 24].

Fig. 1 compares our result to other astrophysical constraints in the low-mass ALP regime. Our most conservative limit exceeds the bounds from extra-galactic supernovae [12] for $m_a < 10^{-10}$ eV, and in our most optimistic ALP flux scenario our limit is comparable to that derived from the non-observation of gamma-rays from SN 1987A [11]. However, the supernova bounds have been questioned due to the modeling of core-collapse supernovae. For $m_a < 10^{-11}$ eV, our limits are superseded by those derived from the lack of spectral variation observed by Chandra in the active galactic nucleus NGC 1275 [15] and in the core of M87 [14]. We caution, though, that more recent analysis shows that these results could be weakened by several orders of magnitude depending on the relative magnitude of the regular and turbulent intracluster magnetic fields that are assumed [16].

We emphasize that since each of these astrophysical constraints has unique sources of systematic error that

may affect the final result, it is worthwhile to survey similar regions of parameter space with multiple techniques. The constraints presented here assume conversion in a homogeneous regular magnetic field, which allows for consistent comparison with previous astrophysical bounds, e.g. SN 1987A [11]. Although the magnetic structure of the Galaxy is certainly more complex, compared to more distant sources, the proximity of Betelgeuse should allow future observations to better constrain the relevant small-scale variations in magnetic structure, especially the ultra-local magnetic fields of the Solar region which are not yet completely mapped (e.g. [28, 50, 51]). The combination of the novel ALP constraint presented here with multiple overlapping astrophysical constraints, each with separate modeling assumptions and uncertainties, builds confidence in the robustness of the exclusion of this corner of parameter space for low-mass ALPs.

We finally comment that a synergy between our astrophysical approach and direct ALP searches might lead to surprises and also unexpected benefits. Indeed, it might be that a future low-mass ALP experiment such as ABRACADABRA [52], DM-Radio [53], or IAXO [23] would discover an ALP in the region where optimistic assumptions on Galactic B -field and stellar model would have led to an exclusion from Betelgeuse. In this case one would come back to our original assumptions. Taking into account the typical uncertainty on the B -field one would give a lower limit on the time until the core-collapse for Betelgeuse, as shown in Fig. 4 for an ALP mass and a coupling in the range $g_{a\gamma} = (5 - 30) \times 10^{-12} \text{ GeV}^{-1}$. Intriguingly ALPs might represent the only possibility to extract such information about the fate of Betelgeuse.

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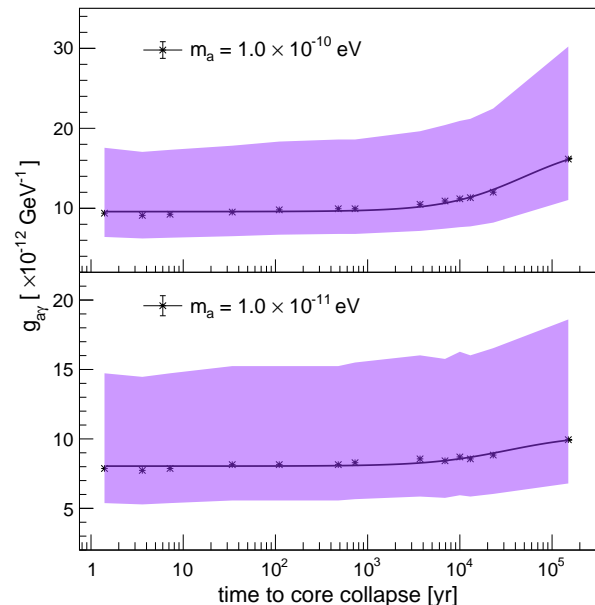


FIG. 4. Evolution on the derived 95% C.L. upper limit of $g_{a\gamma}$ with remaining time until the core-collapse for Betelgeuse. Results are shown for $m_a = 1.0 \times 10^{-11} \text{ eV}$ and $m_a = 1.0 \times 10^{-10} \text{ eV}$ assuming $B_T = 1.4 \mu\text{G}$ (more masses are shown in the Supplementary Material). The solid black line shows the fitting. The width of the violet band indicates the uncertainty due to choice of B_T .

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Supplemental Materials: Constraints on Axion-like Particles from a Hard X-ray Observation of Betelgeuse

BETELGEUSE STELLAR MODELS

The total ALP number per time and energy can be obtained integrating Eq. (2) over the volume of the star, $d\dot{N}_a/dE = \int (d\dot{n}_a/dE)dV$. We find that, with an excellent approximation, the ALP source spectrum has the following form [S57]

$$\frac{d\dot{N}_a}{dE} = \frac{10^{42} C g_{11}^2}{\text{keV s}} \left(\frac{E}{E_0} \right)^\beta e^{-(\beta+1)E/E_0}, \quad (\text{S1})$$

where $g_{11} = g_{a\gamma}/10^{-11} \text{ GeV}^{-1}$, while C is the normalization, E_0 coincides the average energy, and β is the spectrum index. The values of C , E_0 and β depend on various structural parameters characterizing the core of the star, such as temperature, density and chemical composition. To this aim, we will make use of stellar models computed using the FuNS code (see [S25] for a detailed description of this code and the adopted input physics). Alpha Orionis (Betelgeuse) is a red supergiant whose luminosity, effective temperature and metallicity are, respectively, $\log L/L_\odot = 5.10 \pm 0.22$ ([S58]), $T_{\text{eff}} = 3641 \pm 53 \text{ K}$ ([S59]), and $[\text{Fe}/\text{H}] = +0.1 \pm 0.2$ ([S60]). These data constrain the initial mass between 18 and 22 M_\odot , in good agreement with previous determinations ([S61, S62]). We note that the uncertainty of Betelgeuse mass contributes much smaller effect for ALP-photon production than the time to core collapse or B_T , and is thus ignored here. In our analysis we adopted a model of 20 M_\odot with solar composition.

Extant models of stars with mass $\sim 20 M_\odot$ may evolve to the red supergiant stage at the onset or at the end of the core-He burning, depending on the assumed efficiency of the semiconvective mixing (see the discussion in section 2.2 in [S25]). In the FuNS model, scarce semiconvective mixing is usually assumed, so that the star becomes a red supergiant since the beginning of the core-He burning. This phase lasts for $\sim 8 \times 10^5$ yrs, during which the central temperature and density remain more or less the same. After the core He is exhausted, the stellar luminosity increases and attains a maximum value during the C-burning phase. After that, the luminosity remains constant, until the final core collapse. However, during this phase, which lasts a few 10^4 yrs, the temperature and the density within the core undergo constant and substantial increases. In turn, a significant increase of the ALP-production rate is expected (the ALP production rate is a steep function of the temperature).

Since the precise evolutionary status cannot be determined from the observed stellar properties, we have considered a set of stellar models taken at different times before the core-collapse. All of these stellar models match the observed L and T_{eff} . In this way we may trace the expected evolution of the ALP flux during the red supergiant phase of Betelgeuse. The luminosity, the central temperature and the time to the core collapse of these models are reported in Tab. S1. Model 0 assumes Betelgeuse is still in the core-He burning phase; models 1–4 are before C burning; models 5–9 are during the C burning; model 11 is during the Ne burning; and model 12 is at the beginning of the O burning. Fig. S1 illustrates the temperature profiles of some of the 13 models for the most internal 6 M_\odot .

Model	Phase	t_{cc} [yr]	$\log_{10}(L_{\text{eff}}/L_\odot)$	$\log_{10}(T_{\text{eff}}/\text{K})$	C	E_0 [keV]	β
0	He burning	155000	4.90	3.572	1.36	50	1.95
1	before C burning	23000	5.06	3.552	4.0	80	2.0
2	before C burning	13000	5.06	3.552	5.2	99	2.0
3	before C burning	10000	5.09	3.549	5.7	110	2.0
4	before C burning	6900	5.12	3.546	6.5	120	2.0
5	in C burning	3700	5.14	3.544	7.9	130	2.0
6	in C burning	730	5.16	3.542	12	170	2.0
7	in C burning	480	5.16	3.542	13	180	2.0
8	in C burning	110	5.16	3.542	16	210	2.0
9	in C burning	34	5.16	3.542	21	240	2.0
10	between C/Ne burning	7.2	5.16	3.542	28	280	2.0
11	in Ne burning	3.6	5.16	3.542	26	320	1.8
12	beginning of O burning	1.4	5.16	3.542	27	370	1.8

TABLE S1. Models of ALP production from Betelgeuse. The stage of stellar evolution is parameterized by the time remaining until the core collapse for Betelgeuse, t_{cc} . See text for the definition of other parameters.

By folding Eq. (3) from Eq. (2), (4) and (5), the differential photon flux per unit energy arriving at Earth can be

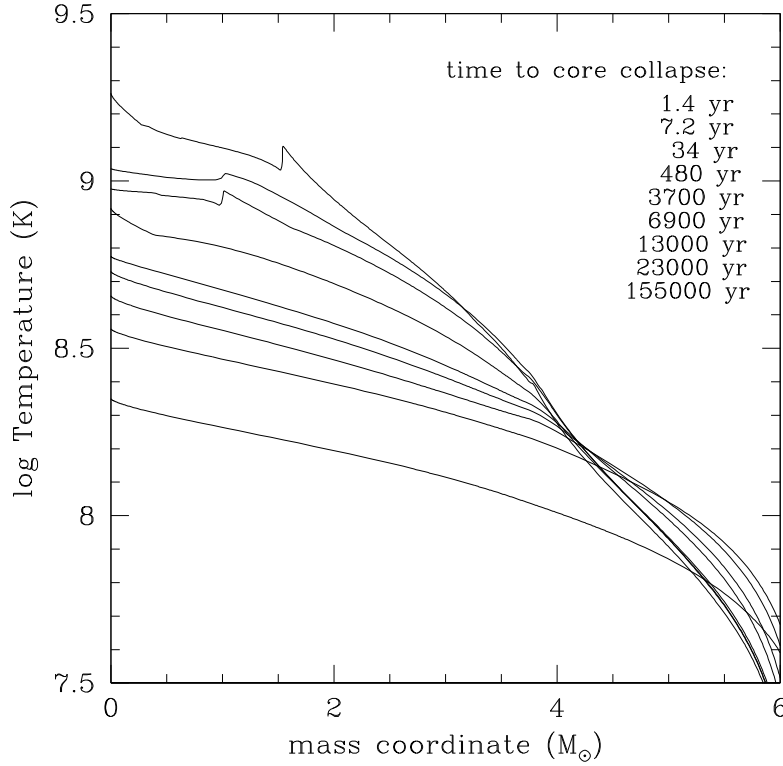


FIG. S1. Temperature profiles of some of the 13 models in Tab. S1. The plot shows the most internal $6 M_{\odot}$ of each model. As the star approaches the final core collapse, the temperature becomes steeper within the core, so that the ALPs production progressively becomes more centrally concentrated. The model labelled 155000 yr to the collapse refers to the He-burning phase, while that 480 yr to the C-burning phase and 1.4 yr to the collapse is taken at the beginning of the O burning. The secondary temperature peaks shown by some models are due to the presence of active C or Ne burning shells.

numerically calculated :

$$\frac{dN_{\gamma}}{dEdSdt} = \frac{g_{11}^4}{\text{keV cm}^2 \text{s}} \left(\frac{C}{5.36 \times 10^5} \right) \left(\frac{E}{E_0} \right)^{\beta} e^{-(\beta+1)E/E_0} \left(\frac{B_T}{1 \mu\text{G}} \right)^2 \left(\frac{d}{197 \text{ pc}} \right) \frac{\sin^2 q}{q^2}, \quad (\text{S2})$$

where

$$q \simeq \left[77 \left(\frac{m_a}{10^{-10} \text{ eV}} \right)^2 - 0.14 \left(\frac{n_e}{0.013 \text{ cm}^{-3}} \right) \right] \times \left(\frac{d}{197 \text{ pc}} \right) \left(\frac{E}{1 \text{ keV}} \right)^{-1},$$

Using the fitted parameters in Tab. S1, Fig. S2 shows the predicated X -ray spectra before and after *NuSTAR* instrument response for typical ALP masses in this work.

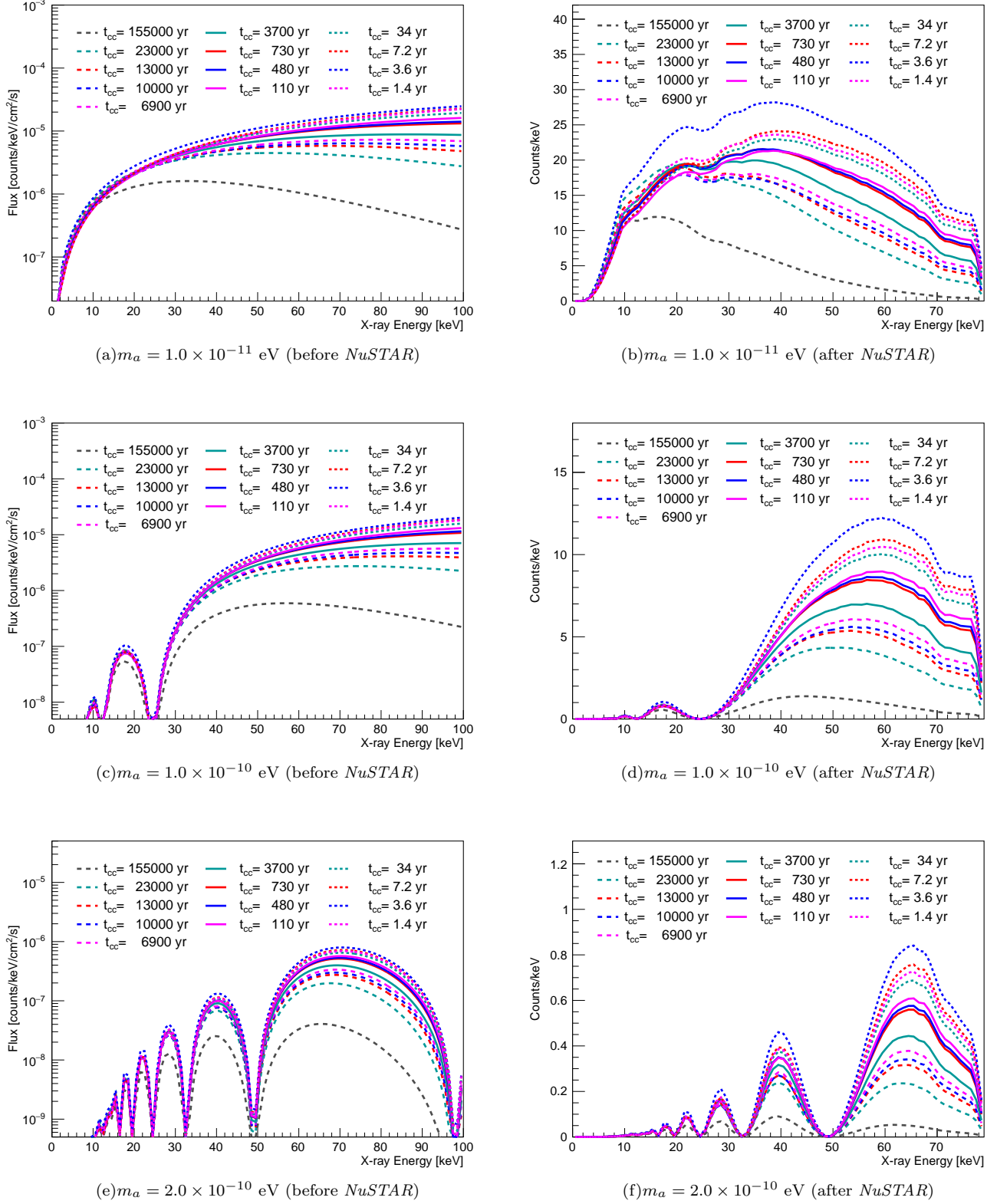


FIG. S2. Predicated X-ray spectra *before* and *after* NuSTAR instrument response with ALP-photon production models for representative ALP masses with assumption of $B_T = 1.4 \mu G$ and $g_{a\gamma} = 1.5 \times 10^{-11} GeV^{-1}$.

NUSTAR BACKGROUND MODELING

The *NuSTAR* instrument background spectral model contains several components, which may be broadly categorized as having astrophysical or detector origins. Our ALP search does not require a detailed parametrization of the *NuSTAR* instrument background, so we summarize the most important aspects here and refer the reader to Refs. [S36, S40] for a detailed description. Our primary concern is the uniformity of the instrument background between the source spectral extraction region and the background spectral extraction region. The background components that are known to have significant spatial variation across the detector arrays are the unfocused *X*-ray background (CXB) and *X*-rays from fluorescence/activation of the instrument structure. The CXB level is observed to be nearly uniform on the sky for the angular and energy acceptance of a single *NuSTAR* observation [S54, S55], but the shadowing effects of the optics bench and aperture stops produce a radially-varying intensity pattern for the unfocused CXB. The intensity of the detector background is known to vary between the detector chips, though is largely constant within each chip [S40]. Both the unfocused CXB gradient and the detector emission motivate the choice of a background region as close as possible to—and ideally on the same detector chip as—the source region, as shown in Fig. S3.

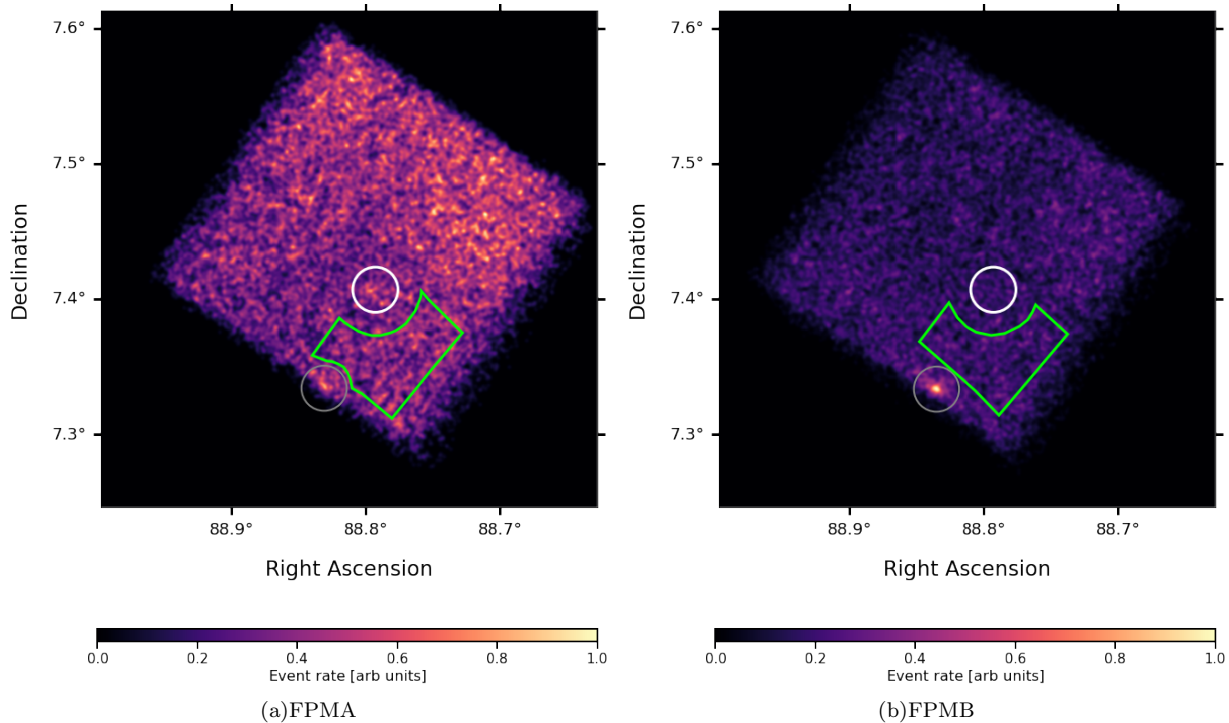


FIG. S3. FPMA (left) and FPMB (right) images of *NuSTAR* observation regions in the energy range 3–79 keV, the event rate in each image is the relative value to the highest one and the image is smoothed with a 2-dimensional Gaussian of width $\sigma = 4.5''$ for presentation. The Betelgeuse source region (white circle, $60''$ radius) and background region (green polygon, at least $120''$ from Betelgeuse) are shown. The far-away point source is indicated with gray circle ($60''$ radius).

We further confirm the spatial uniformity of background by comparing the *X*-ray spectra with different choices of background region on the same detector chip. In addition to the polygon region shown in Fig. S3, we also choose the other two circle regions ($60''$ radius) which are $120''$ away from the Betelgeuse center. Using the data process described above, we extract the *X*-ray spectrum in each background region. Fig. S4 compares the spectra from three background regions after the normalization of region size for FPMA and FPMB. This confirms that our analysis is robust to the exact choice of background spectral extraction region, and that our background region accurately models the instrumental and astrophysical background underlying our source region.

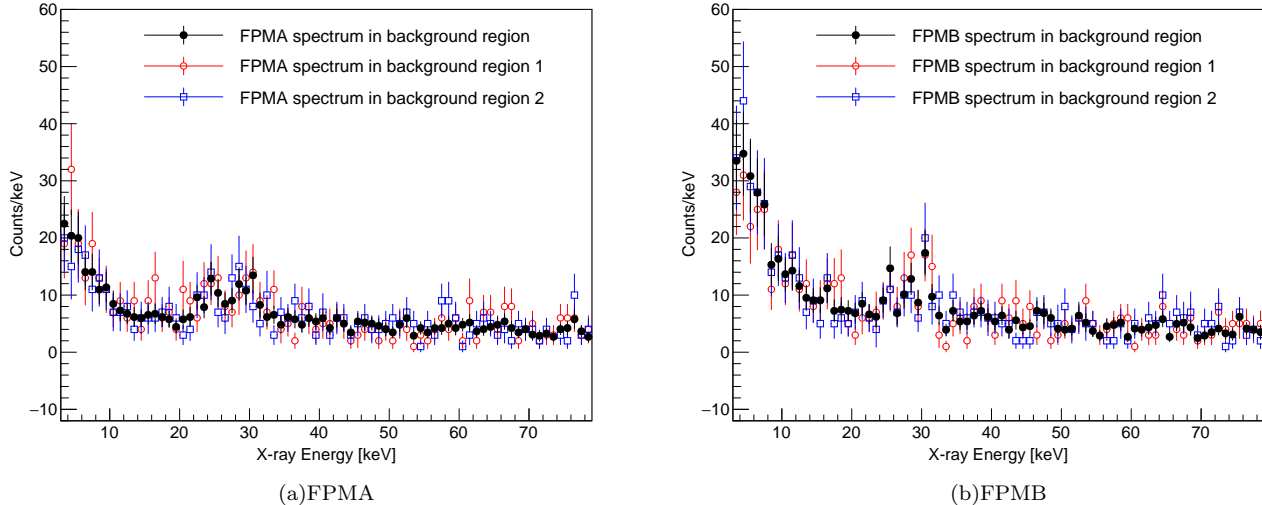


FIG. S4. X-ray spectra in 3–79 keV energy range from FPMA and FPMB in different background regions after the normalization of region size: the black is the spectrum from the polygon region shown in Fig. S3; the red and blue are for the other region choices (see text for details). The data is binned with the width of 1 keV for presentation. The error bars are calculated by Sumw2 with ROOT.

CHANDRA OBSERVATION OF BETELGEUSE

As a cross-check of our results, we use a 5 ks *Chandra* observation of Betelgeuse. *Chandra* has lower, and better understood, instrument background than *NuSTAR*, but its low-energy range (<10 keV) makes it less powerful for constraining the expected ALP-induced spectrum. We thus use the *Chandra* data to verify that our derived 95% C.L. on $g_{a\gamma}$ is consistent with this low-background, low-energy dataset. We analyzed an archival *Chandra* observation, ObsID 3365, which used the ACIS-I configuration in FAINT mode and was taken on 16 December 2001. We reprocessed the data using the standard `chandra_repro` tool from the CIAO v.4.12 software, with updated calibration files (CALDB v4.9.2.0, [S56]). The resultant cleaned data had a 4.899 ks exposure. Fig. S5 shows the observation image for 0.3 – 8 keV soft X-ray events from *Chandra*. The short exposure time and low count rates made analyzing background-subtracted spectra difficult. Rather, we used the new CIAO `aprates` tool, which computes values and limits for various parameters such as point source count rate and photon flux (<https://cxc.harvard.edu/ciao/threads/aprates/index.html>).

Upper limits for the 0.3 – 2.5 keV energy range emission from Betelgeuse for ObsID 3365 were first reported by Posson-Brown et al. (2007) (see Table 4 there). We used the same source ($r = 4''$) and background ($r_{min} = 10''$, $r_{max} = 10''$) regions centered on the star’s equatorial position, and with `aprates` calculated a 3σ upper limit that matched the reported upper limit count rate. We then extended our analysis to the 0.3 – 8 keV energy range. The resultant upper limits are 4.6 counts, or 9.42×10^{-4} counts s^{-1} . By counting the total events in the energy range 0.3 – 8 keV, the constraints on $g_{a\gamma}$ is set as $2.2 \times 10^{-11} GeV^{-1}$ for the most optimistic stellar model and $B_T = 3 \mu G$, and $6.5 \times 10^{-11} GeV^{-1}$ for the most conservative stellar model and $B_T = 0.4 \mu G$ for $m_a < 3.5 \times 10^{-11} eV$. These values are well within our excluded regions, and thus we confirm that our results are consistent with this low-energy dataset.

CONSTRAINTS ON $g_{a\gamma} \times \sqrt{B_T}$

As shown in Eq. S2, the ALP-photon flux scales as $g_{a\gamma}^4 \cdot B_T^2$. To separately discuss the uncertainty from Betelgeuse stellar model (t_{cc}) and magnetic field (B_T), we also present our results as the constraints on the production of $g_{a\gamma}$ and $\sqrt{B_T}$ in Fig. S6. We set a constraint of $1.2 \times 10^{-11} GeV^{-1} \sqrt{\mu G}$ for $m_a < 3.5 \times 10^{-11} eV$ for $t_{cc} = 1.55 \times 10^5$ yr, and $0.9 \times 10^{-11} GeV^{-1} \sqrt{\mu G}$ for $m_a < 5.5 \times 10^{-11} eV$ for $t_{cc} = 3.6$ yr.

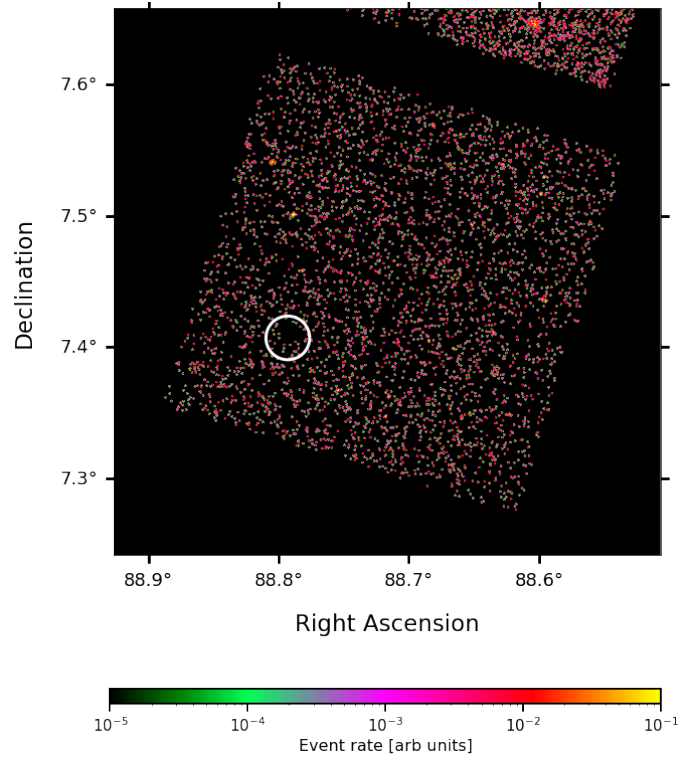


FIG. S5. Observation image for 0.3 – 8 keV soft X -ray events from *Chandra*, the event rate is the relative value to the highest one and the image is smoothed with a 2-dimensional Gaussian of width $\sigma = 4.5''$ for presentation. The Betelgeuse source region is indicated with the white circle.

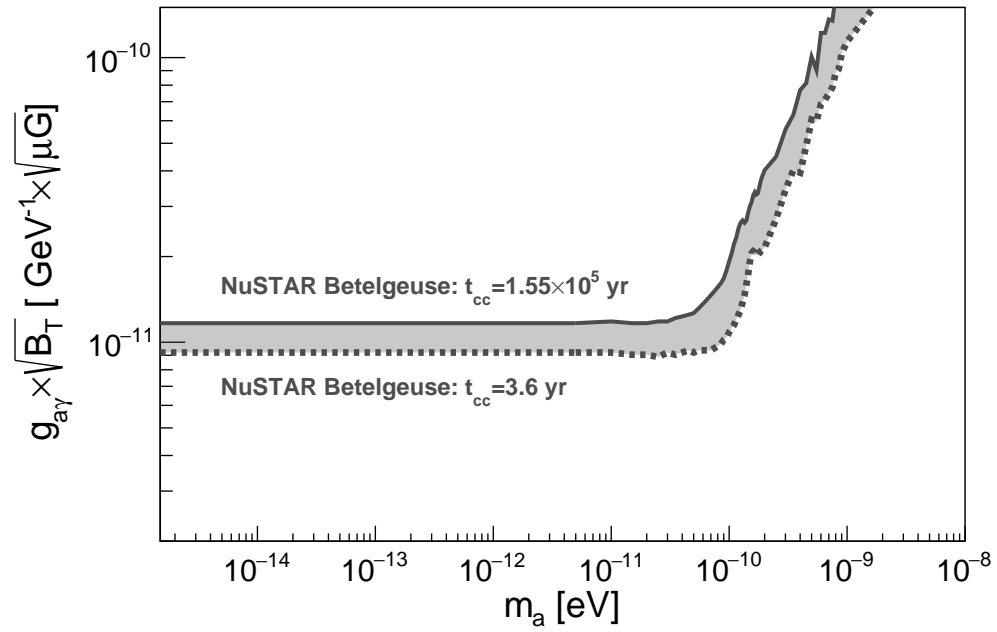


FIG. S6. Upper limits on $g_{a\gamma} \times \sqrt{B_T}$: the solid line is for the most conservative stellar model, dashed line for the most optimistic stellar model and the band for the other models between in.

EVOLUTION OF $g_{a\gamma}$ FOR MORE ALP MASSES

Fig. S7 illustrates the $g_{a\gamma}$ evolution as the remaining time for core collapse of Betelgeuse for more ALP masses.

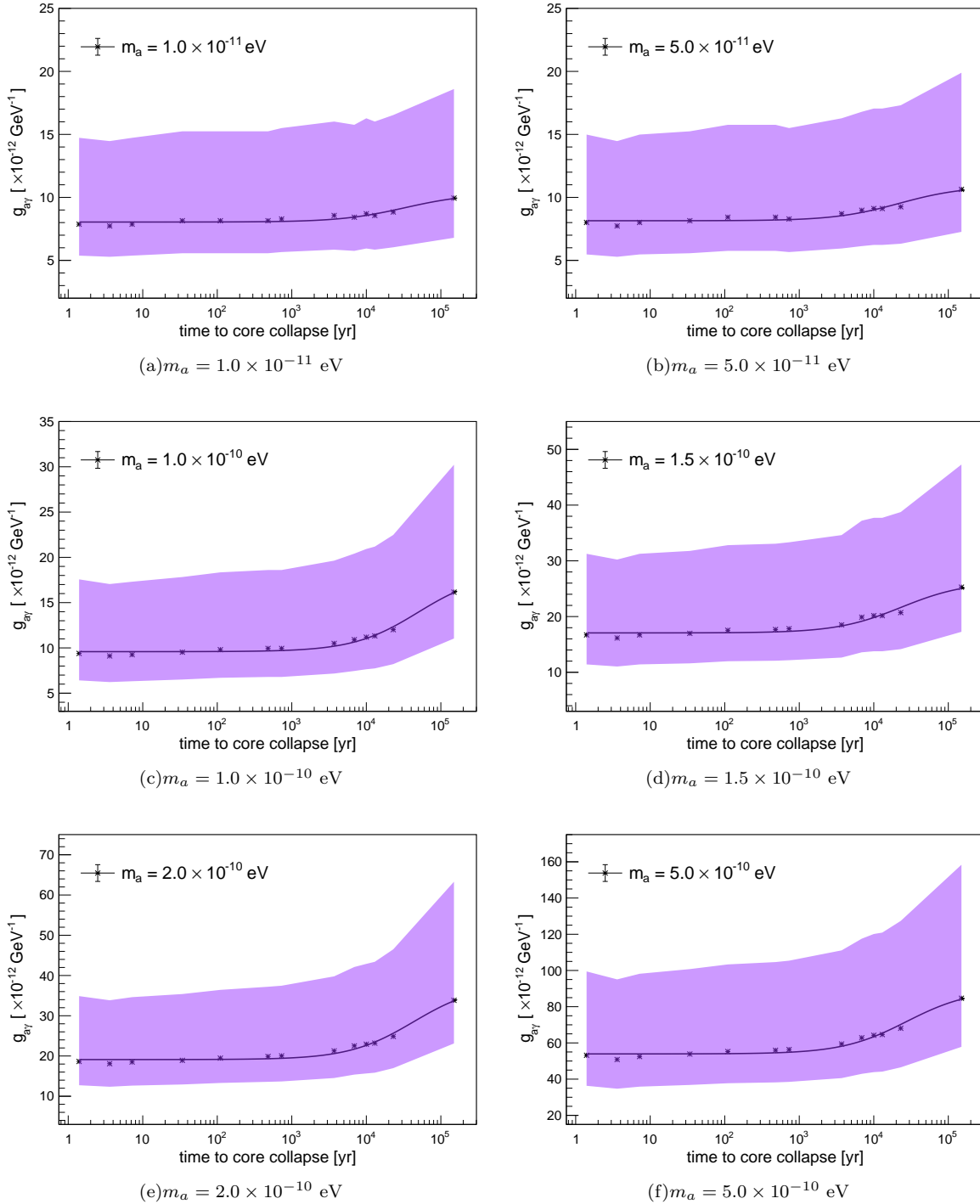


FIG. S7. Evolution on the derived 95% C.L. upper limit of $g_{a\gamma}$ for different ALP masses with remaining time until core collapse for Betelgeuse. The points are the results with the assumption of $B_T = 1.4 \mu G$ and the solid black line shows the fitting. The width of the violet band indicates the uncertainty due to choice of B_T .