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Deep Upper Limit on the Optical Emission during a Hard X-Ray Burst from the Magnetar SGR J1935+2154

Abstract

In 2021 September the magnetar SGR J1935+2154 entered a stage of burst/flaring activity in the hard X-ray band. On 2021 September 10, we observed SGR J1935+2154 with the fiber-fed fast optical photon counter IFI+Iqueye, mounted at the 1.22 m Galileo telescope in Asiago. During one of the IFI+Iqueye observing windows, a hard X-ray burst was detected with the Fermi Gamma-ray Burst Monitor. We performed a search for any significant increase in the count rate on the 1 s, 10 ms, and 1 ms binned IFI+Iqueye light curves around the time of the Fermi burst. No significant peak was detected with a significance above 3σ in an interval of ± 90 s around the burst. Correcting for interstellar extinction ($A_V \simeq 5.8$ mag), the IFI+Iqueye upper limits to any possible optical burst from SGR J1935+2154 are V=10.1 mag, V=7.2 mag, and V=5.8 mag for the 1 s, 10 ms, and 1 ms binned light curves, respectively. The corresponding extinction-corrected upper limits to the fluence (specific fluence) are 3.1×10^{-10} erg cm⁻² (0.35 Jy s), 4.2×10^{-11} erg cm⁻² (4.8 Jy ·10 ms), and 1.6×10^{-11} erg cm⁻² (17.9 Jy ms), orders of magnitude deeper than any previous simultaneous optical limit on a magnetar burst. The IFI+Iqueye measurement can also place a more stringent constraint on the spectral index of the optical to hard X-ray fluence of SGR J1935+2154, implying a spectrum steeper than $\nu^{0.64}$. Fast optical timing observations of bursts associated with radio emission then have the potential to yield a detection.

Unified Astronomy Thesaurus concepts: X-ray bursts (1814); X-ray stars (1823); Photometry (1234)

1. Introduction

SGR J1935+2154 is a Galactic magnetar, a nonaccreting neutron star powered mainly by magnetic energy dissipation (see Mereghetti et al. 2015; Turolla et al. 2015; Kaspi & Beloborodov 2017 for recent reviews). This class of highenergy sources is characterized by strong variability and recurrent bursts of hard X-rays/soft gamma-rays (hence the name soft gamma-ray repeaters, SGRs), that have typical duration $\lesssim 1$ s and peak luminosity $\lesssim 10^{39-41}$ erg s⁻¹. Hyperenergetic bursts with peak luminosity reaching 10^{47} erg s⁻¹, known as giant flares, have also been emitted sporadically by a handful of magnetars (e.g., Palmer et al. 2005).

SGR J1935+2154 was discovered through the detection of a short burst with the Neil Gehrels Swift Observatory/Burst Alert Telescope in 2014 (Stamatikos et al. 2014). Follow-up observations in the X-ray band revealed that the source is a magnetar with spin period $P=3.25\,\mathrm{s}$ and period derivative $\dot{P}=1.43\times10^{-11}\,\mathrm{s}\,\mathrm{s}^{-1}$ (Israel et al. 2016), leading to a characteristic age of 3.6 kyr and a dipole magnetic field of $2.2\times10^{14}\,\mathrm{G}$. A very faint ($H\sim24$) near-infrared counterpart was identified with the Hubble Space Telescope (Levan et al. 2018). No pulsed radio emission has been observed so far (e.g.,

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Tang et al. 2021), although a tentative detection was recently reported (Zhu et al. 2020).

The source is projected in the direction of the Galactic plane and could be associated with the supernova remnant G57.2 \pm 0.8 for which several distance estimates are reported in the literature (see, e.g., Zhou et al. 2020 and references therein). In the following, we will adopt the distance derived from an analysis of the dust-scattering ring observed in X-ray images taken with the Swift X-ray Telescope instrument in 2020 ($d = 4.4^{+2.8}_{-1.3}$ kpc; Mereghetti et al. 2020), which is independent of the supernova remnant association.

SGR J1935+2154 has sporadically gone through phases of hard X-ray burst/flaring activity (e.g., Borghese et al. 2020; Lin et al. 2020a; Younes et al. 2017, 2021). The outburst episode observed in 2020 culminated in tens of bursts emitted in a few days (see, e.g., Mereghetti et al. 2020 and references therein). During this outburst, on 2020 April 28 an extremely bright millisecond-duration radio burst (FRB 200428) was emitted by SGR J1935+2154 and detected with the Canadian Hydrogen Intensity Mapping Experiment (CHIME; CHIME/ FRB Collaboration et al. 2020) and STARE2 (Bochenek et al. 2020) telescopes. The radio burst turned out to be temporally coincident with a bright, hard X-ray burst detected with the International Gamma-Ray Astrophysics Laboratory (INT-EGRAL; Mereghetti et al. 2020), Konus-Wind (Ridnaia et al. 2021), Insight Hard X-ray Modulation Telescope (HXMT; Lin et al. 2020b), and AGILE (Tavani et al. 2021) satellites. No

Table 1
Log of the 2021 September Unfiltered Observations of SGR J1935+2154
Carried out with IFI+Iqueye Mounted at the 1.22 m Galileo Telescope at the
Asiago Astrophysical Observatory

Observation ID	Start Time (UTC)	Exposure (s)	Rate (kc/s)
20210911-002926	2021-09-10 22:39:29.0	1197.4	1.8
20210911-011727	2021-09-10 23:17:30.0	1797.6	2.0
20210911-014851	2021-09-10 23:48:54.0	1797.6	2.3

optical counterpart was detected in a simultaneous observation performed with BOOTES (Lin et al. 2020b) down to an extinction-corrected fluence of \lesssim 4400 Jy ms. A near-infrared campaign was also carried out with the Palomar-Gattini-IR observing system in the *J*-band, placing an upper limit on the second-timescale extinction-corrected fluence of \lesssim 125 Jy ms (De et al. 2020).

In the period between 2021 September 9 and September 22, SGR J1935+2154 entered a new stage of burst/flaring activity, detected with several satellites (GECAM, Xiao et al. 2021; Konus-Wind, Ridnaia et al. 2021; Fermi, Roberts et al. 2021; AGILE, Ursi et al. 2021). We then decided to target the source with our fast photon counter Iqueye (Naletto et al. 2009), which is fiber-fed at the 1.22 m Galileo telescope at the Asiago Astrophysical Observatory through the Iqueye Fiber Interface (IFI; Zampieri et al. 2019). Our main goal was exploiting the exquisite time resolution (up to ns) and high sensitivity of our instrumentation to search for second or sub-second optical flashes possibly associated with X-ray and/or radio bursts from SGR J1935+2154.

The observations presented here are part of a multi-wavelength program devoted to searching for prompt/delayed optical flashes from fast radio bursts (FRBs) and magnetars (e.g., Pilia et al. 2020). In Section 2 we present the observations of SGR J1935+2154 carried out on 2021 September 10 with IFI+Iqueye and the Fermi Gamma-ray Burst Monitor (GBM) instrument. In Section 3 we show the results of the analysis, while in Section 4 we discuss them within the framework of previous measurements.

2. Observations and Data Analysis

2.1. IFI+Iqueye

On the night of 2021 September 10, we observed the area of the sky centered at the position of SGR J1935+2154 (R.A. = 19 $34\ 55.606$, decl. = $+21\ 53\ 47.45$, J2000, error 0."2; Levan et al. 2018) with the fiber-fed fast optical photon counter IFI+Iqueye (Naletto et al. 2009; Zampieri et al. 2019), mounted at the 1.22 m Galileo telescope at the Asiago Astrophysical Observatory. The log of the observations, performed in white light without filters, and the average count rate (not background-subtracted) measured at the position of SGR J1935+2154 are reported in Table 1. At the beginning and at the end of each acquisition, a nearby sky region and a reference star close to the position of the source were also observed to monitor the quality and transparency of the sky. The first 10 minutes of the first observation (Obs. ID 20210911-002926) were affected by passage of slight veils and were then discarded, leaving a useful observing window of \sim 20 minutes.



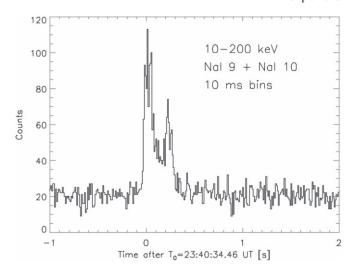


Figure 1. Fermi GBM light curve of the burst detected during the IFI+Iqueye observation. Time is measured from the burst trigger time T_0 . The bin size is 10 ms.

The target was carefully centered on the IFI instrument camera in such a way as to match the position of the optical fiber injecting the light into Iqueye (Zampieri et al. 2019). To this aim, an image of the field was previously acquired and astrometrically calibrated using nine stars in the field. The error of the target position registered on the image is 0.16, significantly smaller than the optical fiber diameter.

The photon event lists acquired with Iqueye were reduced using a dedicated software. Light curves binned at 1 ms, 10 ms, and 1 s were computed from the reduced event lists and searched for any significant rate increase.

2.2. Fermi GBM

In 2021 September, the Fermi GBM instrument revealed several bursts from the direction of SGR J1935+2154 (Roberts et al. 2021). One of them occurred on September 10, during our IFI+Iqueye observations (GBM trigger n. 653010039, at $T_0 = 23:40:34.46$ UTC). Figure 1 shows the 10–200 keV light curve of this burst binned at 10 ms, as derived by summing the counts of the two NaI detectors with the best orientation for the magnetar direction (n. 9 and n. 10).

In order to measure the burst fluence, we performed a spectral analysis by extracting the spectra of the two GBM NaI detectors with the RMFIT software in the time interval $[T_0-0.04\,\mathrm{s},\,T_0+0.38\,\mathrm{s}]$, as well as those of the corresponding background. The latter was estimated by fitting with a linear function the count rates measured in time intervals of about 30 s before and after the burst. We fitted the two spectra simultaneously in the energy range from 10 to 200 keV with an exponentially cutoff power-law function defined as $N(E)=KE^{-\Gamma}e^{-(2-\Gamma)E/E_p}$ photons cm⁻² s⁻¹ keV⁻¹. A good fit was obtained with photon index $\Gamma=0.88^{+0.34}_{-0.38}$, peak energy $E_p=23.5^{+2.2}_{-2.7}$ keV, and flux $F=(7.2\pm0.4)\times10^{-7}$ erg cm⁻² s⁻¹ in the 10–200 keV range. For a burst duration of 0.42 s, this corresponds to a fluence of $(3.0\pm0.2)\times10^{-7}$ erg cm⁻².

¹¹ QUEST v. 1.1.5; see Zampieri et al. (2015).

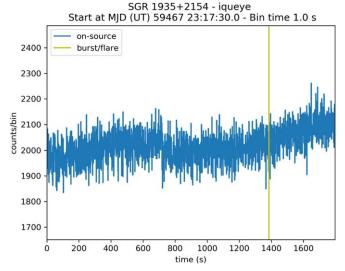


Figure 2. The 1 s binned light curve of the second IFI+Iqueye observation of SGR J1935+2154 performed on 2021 September 10 (Table 1, Obs. ID 20210911-011727). The minute-timescale variations of the count rate are caused by changes in the background sky brightness. The yellow line marks T_0 , the time of arrival of the Fermi GBM burst.

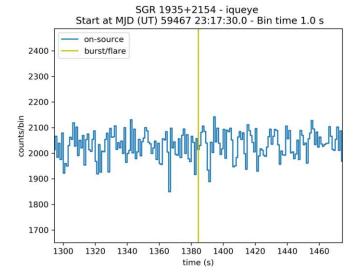
3. Results

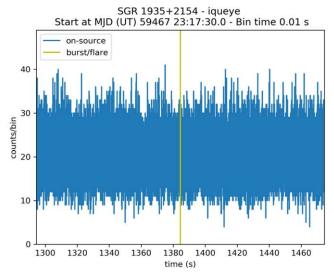
Figure 2 shows the 1 s binned light curve of the second IFI+Iqueye observation. We performed a search for any significant increase in the count rate on the 1 s, 10 ms, and 1 ms binned optical light curves around the time of the Fermi GBM burst.

We assume a Poisson distribution with the average rate of 2030 counts s^{-1} and fix a 3σ detection threshold n_t corresponding to a chance probability of $0.0027/N_{\rm trials}$ in any of the bins during an interval of ± 90 s around T_0 . $N_{\rm trials}$ is the total number of bins in the interval and depends on the bin size. We obtain $n_t = 2220$, 47, 14 counts bin⁻¹ for the 1 s, 10 ms, and 1 ms binned light curves, respectively. No significant peak was detected above n_t in any of the light curves (see Figure 3).

The highest peak in the 1 s binned light curve (2140 counts bin⁻¹) translates into an upper limit to the signal of 230 counts bin⁻¹ at the 3σ confidence level, after subtracting a rate per bin that has a high Poissonian probability (99.73%) to be exceeded by chance in a single bin (1910 counts bin⁻¹). Using the *V*-band calibration of IFI+Iqueye (Zampieri et al. 2016) and taking into account the actual fiber-coupling efficiency at the time of the observation (59%), a value of 230 counts bin⁻¹ corresponds to an average optical brightness over 1 s of V=15.9 mag. Similarly, for the 10 ms and 1 ms binned light curve, the upper limits to the signal in the same interval are 32 counts bin⁻¹ and 12 counts bin⁻¹ (3σ c.1.), respectively, corresponding to an average optical brightness of V=13.1 mag and V=11.6 mag.

We also performed a blind search for any significant increase in the count rate of the 1 s binned light curves of all the IFI+Iqueye observations. During each observation, the count rate changes significantly because the sky diffuse background light increases with decreasing altitude of the target. For this reason, the blind search was performed after removing the increasing-background trend from the data. The upper limits to the signal in the 1 s binned detrended light curves of the three observations are: 290 counts





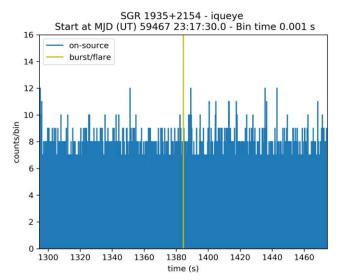


Figure 3. Zooming-in (± 90 s) of the 1 s, 10 ms, and 1 ms binned light curves of the second IFI+Iqueye observation of SGR J1935+2154 performed on September 10, 2021 (Table 1, Obs. ID 20210911-011727). The yellow line marks T_0 , the time of arrival of the Fermi GBM burst. No significant peak is detected around T_0 .

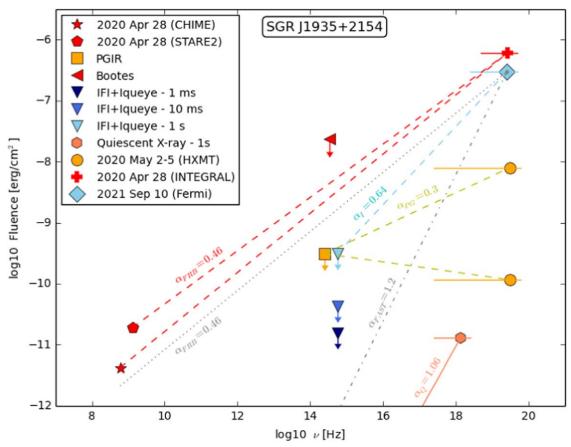


Figure 4. Upper limits to the optical fluence of SGR J1935+2154 during a simultaneous hard X-ray burst detected with Fermi/GBM. The IFI+Iqueye upper limits are extinction-corrected and refer to the 1 s (upper cyan triangle), 10 ms (mid blue triangle) and 1 ms (lower dark blue triangle) binned light curves, respectively. The cyan dashed line shows the lower limit to the spectral index ($\alpha_I = 0.64$) of the optical-gamma-ray fluence of SGR J1935+2154 assuming a power-law spectrum. Also shown are the radio and hard X-ray fluences of the 2020 April 28 burst (CHIME, STARE2, and INTEGRAL measurements), the bursts detected on 2020 May 2-5 (HXMT measurements), the upper limits (extinction-corrected) derived from simultaneous observations in the optical and near-infrared with BOOTES and Palomar-Gattini, respectively, and the corresponding fluence slopes or lower limits ($\alpha_{FRB} = 0.46$ and $\alpha_{PG} = 0.3$, red and yellow dashed lines). The gray lines represent hypotethical power-law dependences for the fluence of the 2021 September 10 event assuming a "2020 April 28"-type burst ($\alpha_{FRB} = 0.46$, dotted line) and a "FAST"type burst ($\alpha_{\text{FAST}} = 1.2$, dotted-dashed line; see text for details). Finally, the orange hexagon and the oblique orange line show the X-ray de-absorbed pre-outburst fluence (Swift measurement, integrated over 1 s) and the fluence slope ($\alpha_0 = 1.06$) of the counterpart of SGR J1935+2154, calculated using the extinction-corrected HST infrared fluence in a quiescent phase.

 bin^{-1} for observation 20210911–002926, 320 counts bin^{-1} for observation 20210911–011727, and 290 counts bin^{-1} for observation 20210911-014851. The corresponding limits to the optical magnitudes are: V = 15.7 mag, V = 15.6 mag, and V =15.7 mag, respectively.

The limits reported above refer to the apparent magnitude and do not take into account the extinction along the line of sight which, for SGR 1935+2154, is significant. We estimate the optical extinction in the direction of SGR J1935+2154 using the interstellar dust maps reported in Green (2018), 12 based on Pan-STARRS and 2MASS photometry and Gaia parallaxes of hundreds of millions of stars (Green et al. 2019). Using these maps and the distance estimate reported in Mereghetti et al. (2020) $(4.4^{+2.8}_{-1.3} \text{ kpc})$, we find a reddening $E(g-r) \simeq 1.8$. The variation of E(g-r) within most of the distance uncertainty range is small (≤ 0.06 mag). Only for a distance larger than 7 kpc, close to the upper boundary, does the reddening increase significantly $(E(g-r) \simeq 2.4)$. From the transformation relations reported in Yuan et al. (2013), we finally derive a V-band extinction of $A_V \simeq 5.8$ mag. This value is smaller but consistent within the uncertainties with the value

The upper limits to the fluence of SGR J1935+2154 measured with IFI+Iqueye and the fluence of the simultaneous hard X-ray burst detected with the Fermi GBM are shown in Figure 4 as a function of frequency. For comparison, we also report the measurements of the fluence of the radio and X-ray burst detected on 2020 April 28 (CHIME/FRB Collaboration et al. 2020; Bochenek et al. 2020; Mereghetti et al. 2020), the

 $A_V \simeq 7.2 \pm 0.9$ mag (De et al. 2020) inferred from the neutral hydrogen column density along the line of sight obtained from

XMM-Newton spectral fittings (Israel et al. 2016), although the

upper limits to any possible optical burst from SGR J1935+2154 in an interval of ± 90 s around T_0 become V = 10.1 mag for the 1 s

binned light curve, V = 7.2 mag for the 10 ms binned light curve,

and V = 5.8 mag for the 1 ms binned light curve. The corres-

Correcting for an extinction $A_V \simeq 5.8$ mag, the IFI+Iqueve

4. Discussion

latter is more uncertain and model-dependent.

fluence of two other X-ray bursts detected a few days later

ponding extinction-corrected upper limits to the fluence (specific fluence) are 3.1×10^{-10} erg cm⁻² (0.35 Jy s), 4.2×10^{-11} erg cm⁻² (4.8 Jy · 10 ms), and 1.6×10^{-11} erg cm⁻² (17.9 Jy ms).

¹² http://argonaut.skymaps.info/

(2020 May 2–5) with HXMT (Lin et al. 2020b), and the X-ray de-absorbed fluence (Swift measurement, integrated over 1 s; Israel et al. 2016) of the quiescent (pre-outburst) counterpart of SGR J1935+2154.

We note that the radio to hard X-ray fluence ratio for the 2020 April 28 burst from SGR J1935+2154 is $\approx 10^{-5}$, while the limits for extragalactic FRBs imply a ratio $\gtrsim 10^{-(9\div10)}$ (Nicastro et al. 2021; see also the limit of $>10^{-9}$ for the closest extragalactic FRB in M81, Mereghetti et al. 2021). Both on April 28 and on May 2–5 there were simultaneous observations in the optical or near-infrared bands at low time resolution ($\sim \! 1$ s or larger): with the BOOTES telescope (Lin et al. 2020b, the former) and with the Palomar-Gattini telescope (De et al. 2020, the latter; see again Figure 4).

The results presented here appear to fit well within the framework of previous measurements and, at the same time, provide more stringent constraints on any possible optical impulsive counterpart to the SGR J1935+2154 bursts. Interestingly, the 2020 April 28 burst and that revealed with Fermi have comparable fluences. However, the 1 s IFI+Iqueye upper limit (extinction-corrected) is two orders of magnitude deeper than the previous limit obtained with the BOOTES telescopes. We also note that the BOOTES limit was obtained with an integration time of 60 s. Our inferred limit to the optical to gamma-ray fluence ratio is $R_{\gamma, \text{opt}} \lesssim 10^{-3}$. This value is consistent with the extinction-corrected fluence ratio observed in SGR J1935+2154 and other X-ray pulsars during long-term (~days to weeks) correlated X-ray/near-infrared outbursts ($R_{\text{X,NIR}} \sim 10^{-4}$, e.g., Levan et al. 2018).

The mechanism producing magnetar bursts is still debated. They can be associated with the fast acceleration of magnetospheric particles after spontaneous magnetic field reconnection (see Lyutikov 2003; Woods et al. 2005; see also Elenbaas et al. 2016), or to emission from a magnetically confined pair fireball, driven by the conversion into a hot, optically thick electron-positron plasma of large-amplitude magnetospheric oscillations (Thompson & Duncan 1995, 2001). The spectral properties of the burst radiation have been investigated in some detail for the latter scenario, although a number of open issues still remain (Lyubarsky 2002; Yang & Zhang 2015; van Putten et al. 2016; Taverna & Turolla 2017). Emission from the fireball itself is thermal, likely described by the superposition of two blackbodies, at an effective temperature of $\approx 10 \text{ keV}$, in agreement with observations (see, e.g., the analysis of the "burst forest" of SGR J1900+14 by Israel et al. 2008). Accordingly, no low-energy emission should be expected in a burst. However, energetic photons from the hot pair plasma heat the neutron star surface, ablating material which is then carried away in the form of a baryon-rich outflow, as first pointed out by Thompson & Duncan (2001; see also van Putten et al. 2016), giving rise to a much more complicated picture.

It has been recently suggested that the ultrarelativistic blast wave produced by the interaction of the plasmoid ejected in a magnetar (giant) flare with the magnetar wind in the tail of a previous flare can result in an optical flash via (incoherent) synchrotron emission (Beloborodov 2020; Chen et al. 2020). The energetics of the burst considered here are much below that of a giant flare, so it is unclear whether these considerations still hold. However, by applying to SGR J1935+2154 the scaling between the optical and the total energy released in the burst proposed by Beloborodov (2020), the expected optical fluence is $\approx 10^{-2}$ - 10^{-4} , the high-energy one, depending on the

magnetization parameter of the wind. Our present upper limit, $R_{\gamma,\text{opt}} \sim 10^{-3}$, would still be compatible with such a picture, possibly pointing to a somewhat large magnetization.

The IFI+Iqueye measurement can also place a more stringent constraint on the spectral index of the optical to gamma-ray fluence of SGR J1935+2154. Assuming hereafter a single power-law dependence for the fluence $\tilde{F}_{\nu} \propto \nu^{\alpha}$, the index has to be larger than $\alpha_I = 0.64$ to be consistent with the optical nondetection (see Figure 4). Interestingly, the optical limit lies above the extrapolation of the GBM spectral fit (for which $\alpha = 2 - \Gamma = 0.78 \div 1.5$, where $\Gamma = 0.5 \div 1.22$; see Section 2.2). While the Palomar-Gattini near-infrared fluence limit is similar to that obtained with IFI+Iqueye, the simultaneous X-ray burst detected with HXMT was weaker than the Fermi one and the inferred limit on the slope of the fluence was less constraining ($\alpha_{PG} = 0.3$, De et al. 2020). Similarly, the BOOTES upper limit was not sufficiently deep to even rule out a single power law with the spectral index calculated from the simultaneous radio-gamma-ray detections of FRB 200428 ($\alpha_{\text{FRB}} = 0.46$). For comparison, we also report the fluence slope ($\alpha_Q = 1.06$) of the counterpart of SGR J1935 +2154, calculated using the de-absorbed pre-outburst Swift X-ray fluence $(1.28 \times 10^{-11} \text{ erg cm}^{-2}, \text{ Israel et al. } 2016)$ and the extinction-corrected quiescent Hubble Space Telescope (HST) infrared fluence $(1.19 \times 10^{-15} \text{ erg cm}^{-2})$, Levan et al. 2018), both integrated over 1 s. For this purpose, we neglected the long timescale variability of the infrared source and considered only the dimmest reported measurement (Levan et al. 2018; Lyman et al. 2021). The fluence slope of the counterpart is somewhat steeper than the one that IFI+Iqueye can probe in cases where optical outbursts of comparable magnitude accompany the X-ray bursts.

Evidence for a steep spectral index for some bursts was also reported by Lin et al. (2020b). They found that 29 bursts from SGR J1935+2154 detected with Fermi GBM were not simultaneously detected in the radio band with FAST. The inferred limit to the radio fluence for these bursts implies a rather steep spectral index for the radio to gamma-ray fluence ($\alpha_{\text{FAST}} = 1.2$, Lin et al. 2020b) for the majority of the bursts from SGR J1935+2154. This fact led De et al. (2020) to conclude that the Palomar-Gattini near-infrared measurements would not be sufficiently deep to detect possible counterparts of the majority of the bursts.

If we assume that there are two types of bursts in SGR J1935 +2154, the rarer "2020 April 28"-type bursts and the more common "FAST"-type bursts, and that they are characterized by a single power-law dependence for the fluence, there are two important consequences for the reported measurements. First, the IFI+Iqueye nondetection of the Fermi 2021 September 10 burst is consistent with the "FAST"-type event, as the FAST limit on the fluence slope ($\alpha_{\text{FAST}} = 1.2$) is steeper than that from IFI+Iqueye $(\alpha_I = 0.64)$ and hence the extrapolation of the FAST power-law dependence is expected to fall below the 1 s optical upper limit (dotted-dashed line in Figure 4). Indeed, if the majority of the bursts from SGR J1935+2154 are of the "FAST"-type, they will not be detectable with IFI+Iqueye. Conversely, in the same assumptions, a smaller number of "2020 April 28"-type bursts, characterized by a much flatter radio-through-hard-X-ray slope $(\alpha_{FRB} = 0.46)$, are, in principle, detectable in the optical band with a simultaneous IFI+Iqueye observation, because the extrapolation of the power-law dependence for the 2020 April 28 fluence is above the 1 s IFI+Iqueye upper limit (dotted line in Figure 4).

Therefore, future observations with fast photometers like IFI+Iqueye, simultaneous with "2020 April 28"-type radio+X-ray bursts, have the potential to yield an optical detection. Even if this type of burst is rare, these findings represent a strong motivation for undertaking dedicated fast optical timing campaigns during future outburst episodes of SGR J1935+2154.

Finally, we note that, as shown in Figure 4, the IFI+Iqueye upper limit to the fluence for 10 ms and 1 ms optical bursts is a factor of 7 and 20, respectively, deeper than that of the 1 s binned light curve. While these are not the typical durations of the bursts from SGR J1935+2154, in the future it will be interesting to investigate what limits can be derived by comparing the fluence of 1–10 ms substructures in the radio, X-ray, and gamma-ray bursts with simultaneous fast optical timing observations on these (or even shorter) timescales.

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Facilities: Galileo Telescope Asiago(IFI+Iqueye), Fermi (GBM).

Software: MATPLOTLIB (Hunter 2007), NUMPY (van der Walt et al. 2011) ASTROPY (Astropy Collaboration et al. 2018). ASTROQUERY (Ginsburg et al. 2019).

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